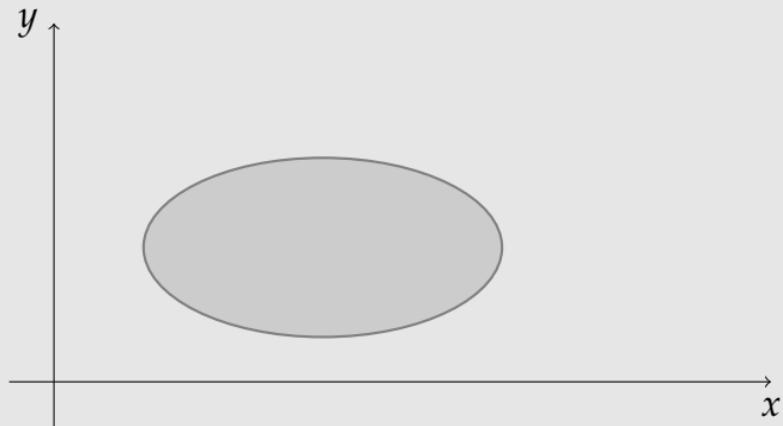


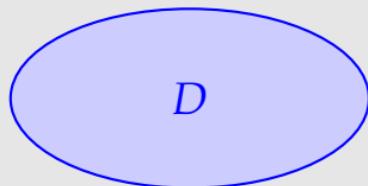
$$\iint_D f(x, y) dx dy$$



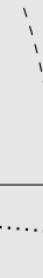
$$\iint_D f(x, y) dx dy$$

y

Ett begränsat område i \mathbf{R}^2 .



R



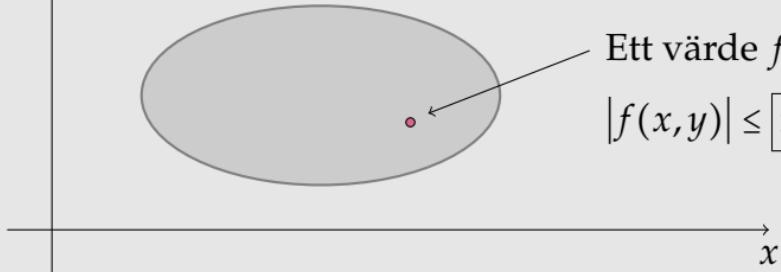
Ryms inuti någon cirkel $x^2 + y^2 = R^2$.

x

$$\iint_D f(x, y) dx dy$$

y

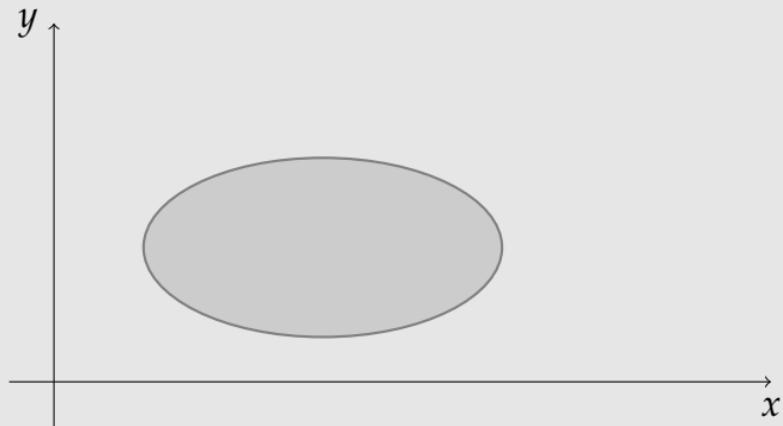
En begränsad funktion på D .



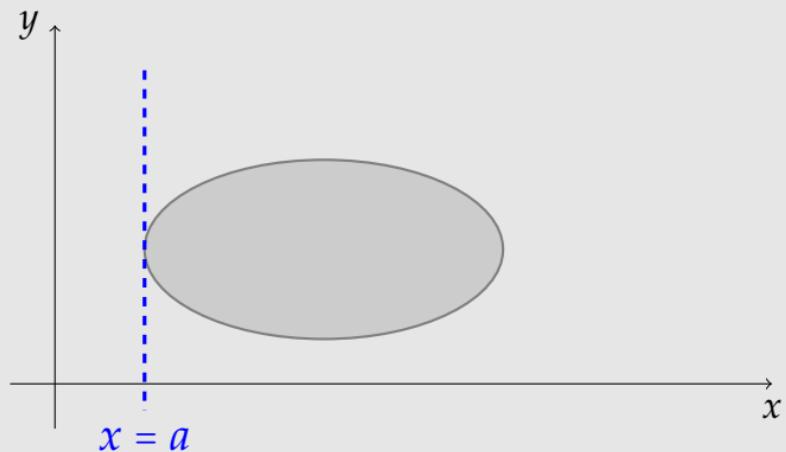
Ett värde $f(x, y)$ i varje punkt $(x, y) \in D$.

$|f(x, y)| \leq [\text{någon konstant}]$ för alla $(x, y) \in D$.

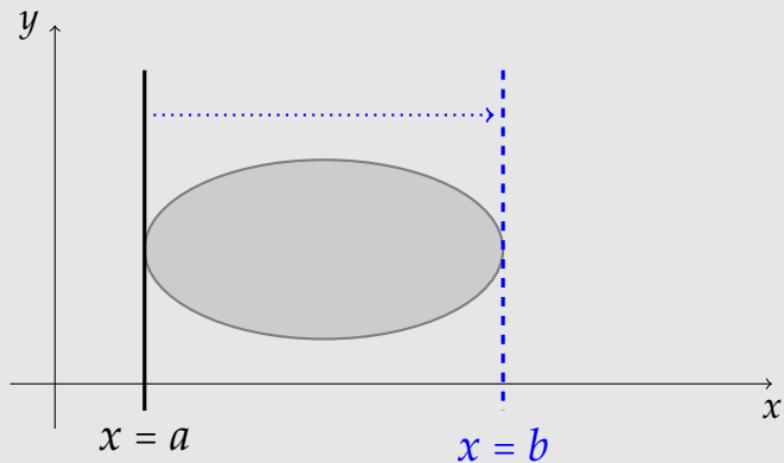
$$\iint_D f(x, y) \, dx \, dy = \int \left(\quad \right) dx$$



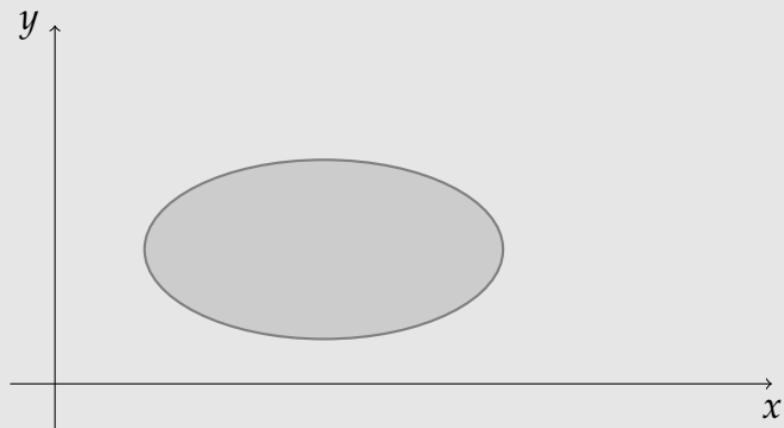
$$\iint_D f(x, y) dx dy = \int_a \left(\right) dx$$



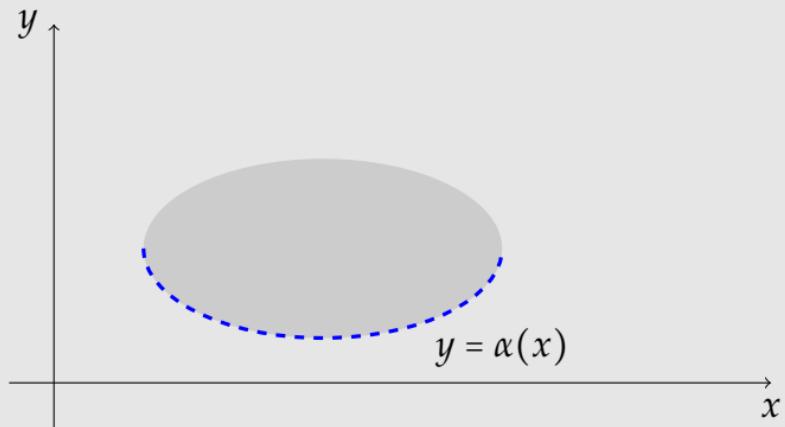
$$\iint_D f(x, y) dx dy = \int_a^{\textcolor{blue}{b}} \left(\quad \right) dx$$



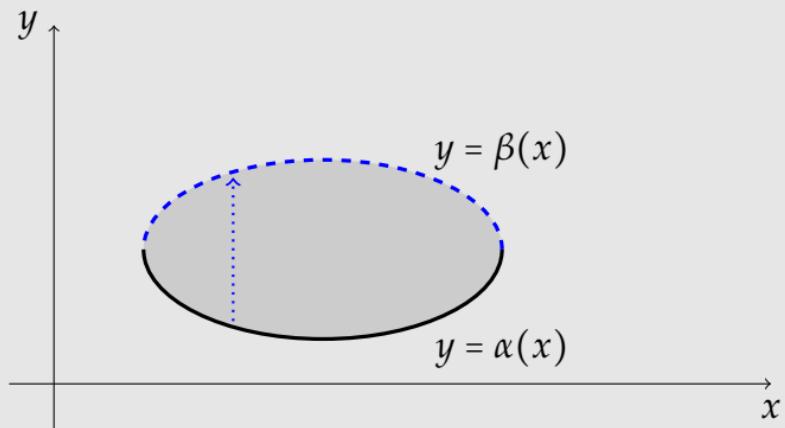
$$\iint_D f(x, y) dx dy = \int_a^b \left(\int$$



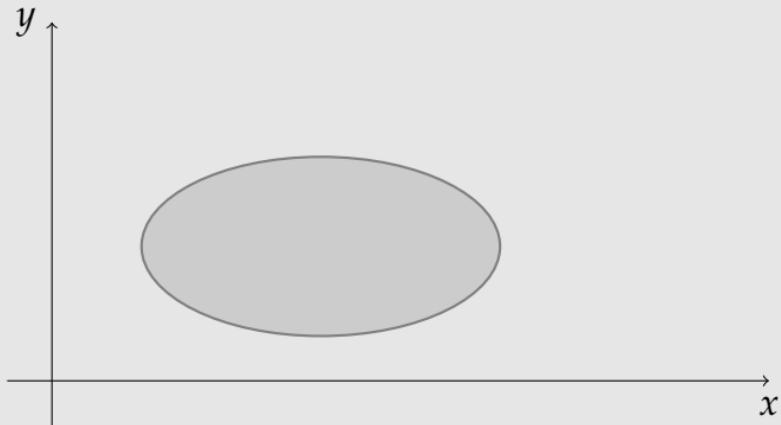
$$\iint_D f(x, y) dx dy = \int_a^b \left(\int_{\alpha(x)}^b dy \right) dx$$



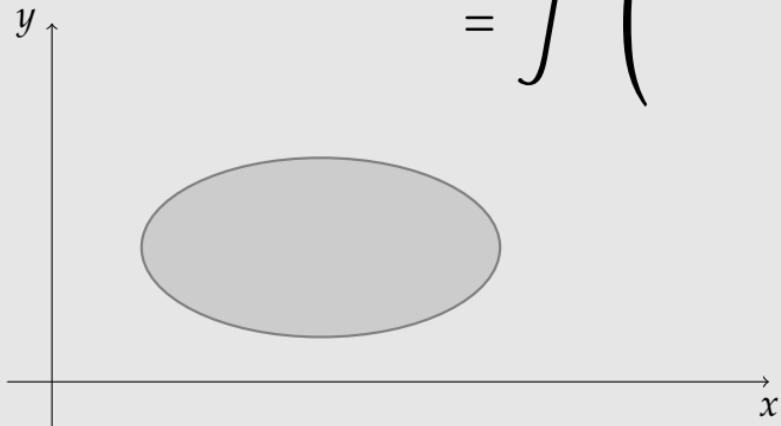
$$\iint_D f(x, y) dx dy = \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} dy \right) dx$$



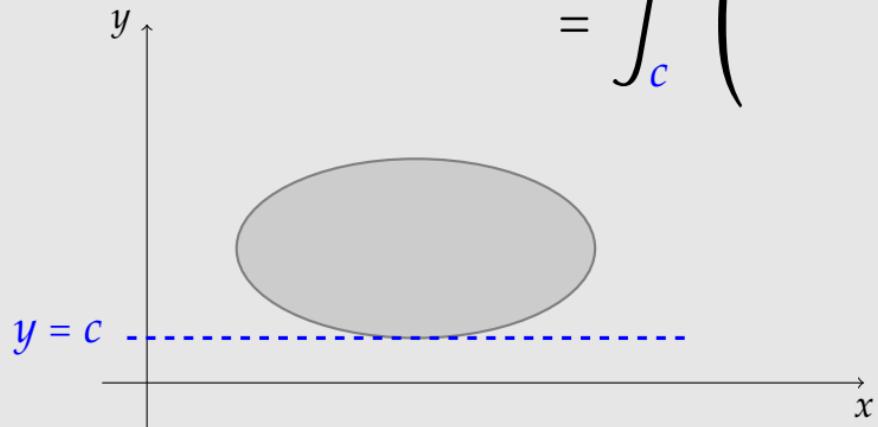
$$\iint_D f(x, y) dx dy = \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) dy \right) dx$$



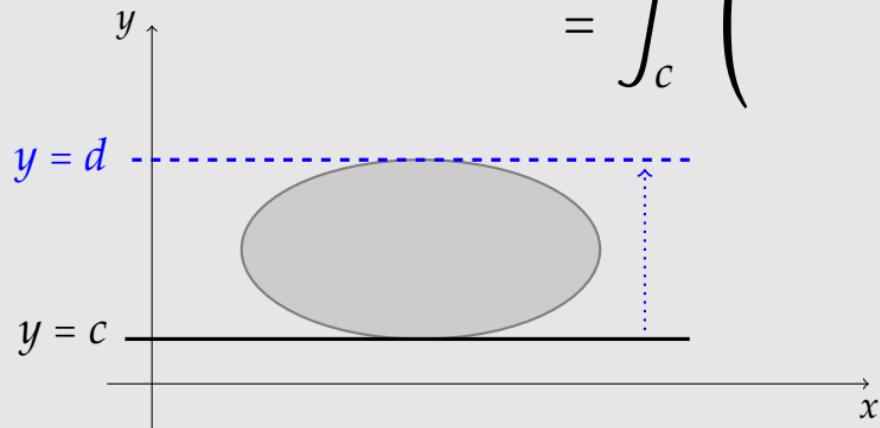
$$\begin{aligned}\iint_D f(x, y) dx dy &= \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) dy \right) dx \\ &= \int \left(\quad \right) dy\end{aligned}$$



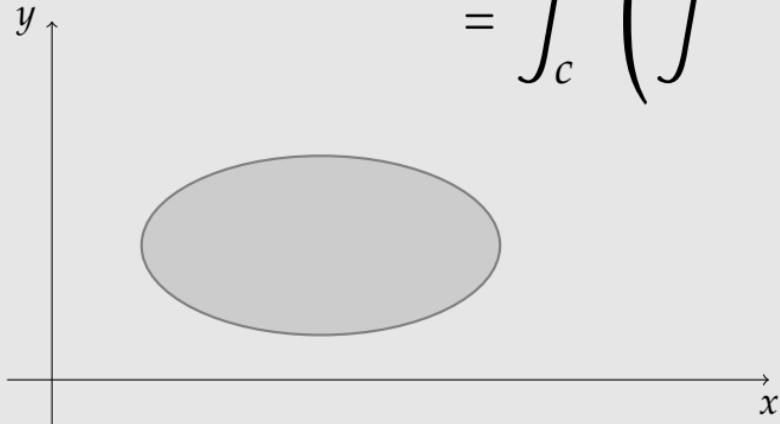
$$\iint_D f(x, y) dx dy = \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) dy \right) dx$$
$$= \int_{\textcolor{blue}{c}} \left(\right) dy$$



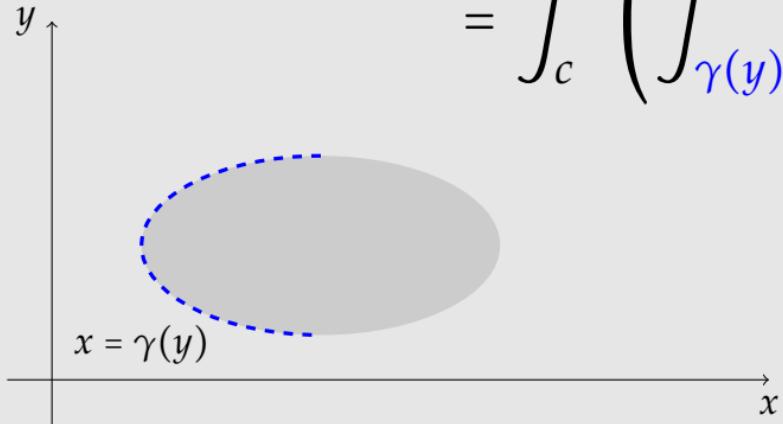
$$\iint_D f(x, y) dx dy = \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) dy \right) dx$$
$$= \int_c^d \left(\right) dy$$



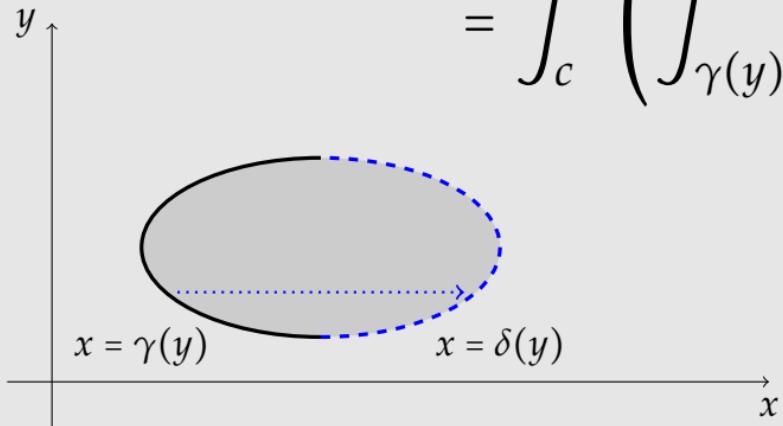
$$\begin{aligned}\iint_D f(x, y) dx dy &= \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) dy \right) dx \\ &= \int_c^d \left(\int \quad \quad \quad dx \right) dy\end{aligned}$$



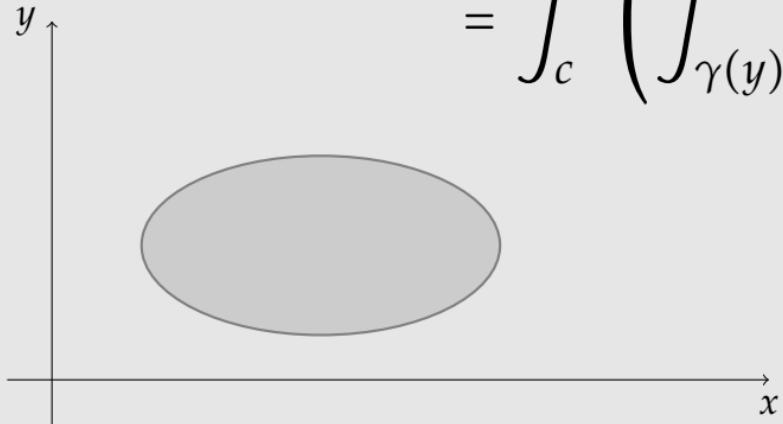
$$\begin{aligned} \iint_D f(x, y) dx dy &= \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) dy \right) dx \\ &= \int_c^d \left(\int_{\gamma(y)}^{\beta(y)} f(x, y) dx \right) dy \end{aligned}$$

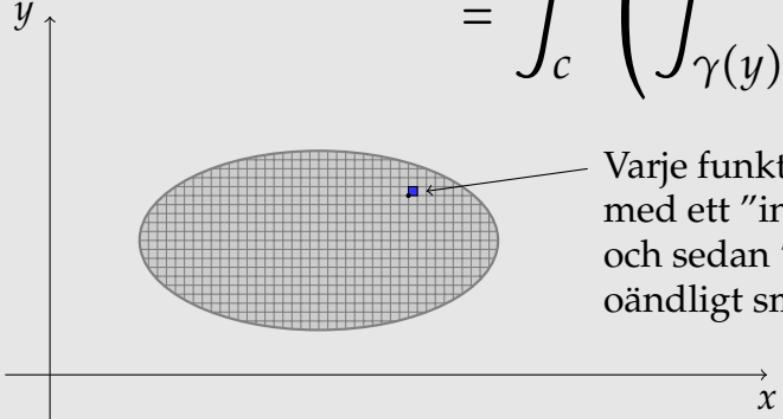


$$\begin{aligned} \iint_D f(x, y) dx dy &= \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) dy \right) dx \\ &= \int_c^d \left(\int_{\gamma(y)}^{\delta(y)} f(x, y) dx \right) dy \end{aligned}$$



$$\begin{aligned}\iint_D f(x, y) dx dy &= \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) dy \right) dx \\ &= \int_c^d \left(\int_{\gamma(y)}^{\delta(y)} f(x, y) dx \right) dy\end{aligned}$$



$$\begin{aligned}
 \iint_D f(x, y) \, dx \, dy &= \int_a^b \left(\int_{\alpha(x)}^{\beta(x)} f(x, y) \, dy \right) dx \\
 &= \int_c^d \left(\int_{\gamma(y)}^{\delta(y)} f(x, y) \, dx \right) dy
 \end{aligned}$$


Varje funktionsvärde $f(x, y)$ multipliceras med ett "infinitesimalt" areaelement $dA = dx \, dy$, och sedan "summeras" dessa oändligt många oändligt små termer $f(x, y) \, dA$.